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U.S. DEPARTMENT OF COMMERCE/National Bureau of Standards

## Calibrating A Six-Port Reflectometer with Four Impedance Standards

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# CONTENTS

	<u>Page</u>
I. INTRODUCTION .....	1
II. SIX-PORT REFLECTOMETER EQUATIONS .....	2
III. CALIBRATION EQUATIONS, a AND b PARAMETERS .....	3
A. Iterative Solution for the $G_i$ .....	3
B. Initial Estimate of the $G_i$ .....	5
IV. EQUATIONS FOR $\Gamma$ .....	6
A. Iterating to Find $\Gamma'$ and $\Gamma''$ : .....	6
B. Linear Solution for $\Gamma'$ , $\Gamma''$ , and $ \Gamma ^2$ .....	7
C. Constant Matrix Solution for $\Gamma'$ , $\Gamma''$ , and $ \Gamma ^2$ .....	8
D. Comparison of Solutions for $\Gamma$ .....	8
V. CALIBRATION EQUATIONS, v and i PARAMETERS .....	9
VI. SIMPLIFIED CALIBRATION EQUATIONS .....	10
A. Ideal Short .....	10
B. Ideal Open, Reactance, and Resistance .....	10
C. Initial Estimates of $H_3$ .....	11
VII. EQUATIONS FOR Z .....	12
A. Constant Matrix Solution for R, X, and $ z ^2$ .....	12
VIII. CONCLUSION .....	13
IX. REFERENCES .....	14
APPENDIX A .....	15





## Calibrating a Six-Port Reflectometer with Four Impedance Standards

Cletus A. Hoer

This report is a theoretical study showing how four terminations of known impedance can be used to calibrate a six-port reflectometer for measuring other terminations of unknown impedance. The equations for obtaining the calibration constants are exact but nonlinear, requiring an iterative solution. Several ways are described for using these constants to calculate the impedance of terminations being measured with the six-port reflectometer.

Key Words: Calibration; impedance; reflection coefficient; reflectometer; six-port.

### I. INTRODUCTION

A six-port reflectometer is a circuit with six ports designed to measure power and reflection coefficient at one of its ports in terms of power readings taken at four other ports when a signal is applied at the remaining port. To measure reflection coefficients with a six-port, it must first be calibrated to determine 11 constants which characterize the six-port. This paper describes a technique for determining these constants with four different terminations whose reflection coefficients are known.

Several techniques have already been published for calibrating a six-port reflectometer. Engen [1,2] has described a technique using a sliding short and a sliding load. However, at frequencies below about 100 MHz, it becomes impractical to use sliding components because their length becomes too long. It then becomes more practical to use fixed terminations which have known values of impedance. A technique for calibrating a pair of six-port reflectometers is described by Hoer [3]. This technique also becomes impractical below about 100 MHz because the standard transmission line used in the calibration procedure becomes too long. Additional work by Engen [2] has shown that it is possible to calibrate a six-port reflectometer with only three known terminations if one first reduces the six-port to an equivalent four-port. This reduction requires that the six-port sidearm power readings be recorded when a minimum of five but preferably nine different unknown terminations are connected to the reference plane. Three of this set of five to nine terminations can be the three known standard terminations. Cronson and Susman [4] have published equations for use in calibrating a six-port reflectometer with four known terminations. Their solution is a closed linear solution, but it assumes that the wave incident upon each of the four terminations is the same when they are connected to the reference plane. This assumption is not usually satisfied. The calibration procedure described below in this paper also uses four known terminations, but the solution for the calibration constants does not require that the incident wave be held constant. However, the equations then become nonlinear, requiring a solution which is an iteration of an approximate linear solution.

This report should be viewed as a preliminary theoretical study. Further work needs to be done to determine the relative merits of the different proposed solutions.

## II. SIX-PORT REFLECTOMETER EQUATIONS

Let the six-port power detectors be labeled as shown in figure 1. It has been shown [3] that the power  $P_i$  measured at port  $i = 3,4,5,6$  is given by

$$P_i = |A_i a + B_i b|^2 \quad i = 3 \dots 6, (1)$$

where  $a, b$  are the waves incident upon, and reflected from, the termination at the measurement reference plane, and  $A_i, B_i$  are functions of the scattering parameters of the six-port and the reflection coefficients of its four power detectors. Engen [5,6] has rewritten eq (1) in the form

$$P_i = |B_i a|^2 |\Gamma - q_i|^2, \quad i = 3 \dots 6, (2)$$

where  $\Gamma$  is the reflection coefficient of the termination at the reference plane, and the  $q_i$  are new constants describing the six-port;

$$\Gamma = b/a, \quad q_i = -A_i/B_i. \quad (3)$$

The four complex  $q_i$  and three of the four  $|B_i|$  are the 11 constants needed to calculate an unknown  $\Gamma$  from the four power readings.

For this paper it will be more convenient to write eq (1) in the form

$$P_i = |A_i a|^2 |1 + G_i \Gamma|^2, \quad i = 3 \dots 6, (4)$$

where

$$G_i = B_i/A_i = -1/q_i.$$

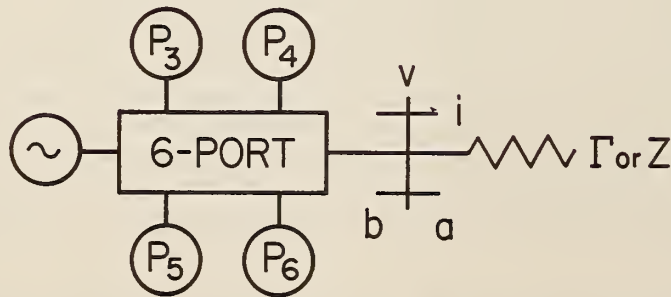


Figure 1. Six port reflectometer.



### III. CALIBRATION EQUATIONS, a AND b PARAMETERS

The calibration is performed by recording each of the four  $P_i$  when four different terminations having known reflection coefficients are connected to the reference plane. Add a subscript  $\ell = 1, 2, 3, 4$  to  $P_i$ ,  $a$ , and  $\Gamma$  in eq (4) to indicate these four known terminations.

$$P_{i\ell} = |A_i a_\ell|^2 |1 + G_i \Gamma_\ell|^2, \quad \begin{matrix} i = 3 \dots 6; \\ \ell = 1 \dots 4. \end{matrix} \quad (5)$$

Let the six-port be designed and the sidearms numbered so that  $P_3$  is primarily a function of the incident wave  $a$ . Then  $P_3$  will never be zero and we can divide eq (5) by  $P_{3\ell}$  to get

$$\frac{P_{i\ell}}{P_{3\ell}} = \frac{|A_i|^2 |1 + G_i \Gamma_\ell|^2}{|A_3|^2 |1 + G_3 \Gamma_\ell|^2} \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 1 \dots 4. \end{matrix} \quad (6)$$

This ratio eliminates  $|a_\ell|$  so that no assumption about the incident wave needs to be made in the calibration process.

For the first termination, eq (6)' gives

$$\frac{P_{i1}}{P_{31}} = \frac{|A_i|^2 |1 + G_i \Gamma_1|^2}{|A_3|^2 |1 + G_3 \Gamma_1|^2} \quad i = 4, 5, 6. \quad (7)$$

Choose the first termination so that its reflection coefficient  $\Gamma_1$ , is such that none of the  $P_{i1}$  are zero. For most existing six-port reflectometer designs, if  $\Gamma_1 \approx 0$ , none of the  $P_{i1}$  will be zero. Then dividing eq (6) by eq (7) gives

$$\delta_{i\ell} \equiv \frac{P_{i\ell} P_{31}}{P_{3\ell} P_{i1}} = \frac{|1 + G_i \Gamma_\ell|}{|1 + G_3 \Gamma_\ell|} \cdot \frac{1 + G_3 \Gamma_1}{|1 + G_i \Gamma_1|}, \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4, \end{matrix} \quad (8)$$

where the  $\delta_{i\ell}$  are calculated from the observed power readings. There are nine equations like eq (8) which can be solved for the four complex constants  $G_3 \dots G_6$  (8 real unknowns). The equations are nonlinear and in general an iteration procedure must be used to solve for the unknowns.

When  $\Gamma_1 \approx 0$ , the remaining three terminations should be highly reflecting and have values of  $\Gamma$  whose phase angles are preferably in different quadrants.

#### A. Iterative Solution for the $G_i$

To simplify the solution of eq (8) for the four  $G_i$ , define

$$g_{i\ell} \equiv |1 + G_i \Gamma_\ell|^2, \quad i = 3 \dots 6, \quad (9)$$

and let the components of  $G_i$  and  $\Gamma_\ell$  be

$$G_i \equiv G_i' + j G_i'', \quad i = 3 \dots 6, \quad (10)$$

$$\Gamma_{\ell} \equiv \Gamma_{\ell}' + j \Gamma_{\ell}'', \quad \ell = 1 \dots 4. \quad (11)$$

Expanding eq (9) with eq (10) and eq (11) leads to

$$g_{i\ell} = |1 + G_i \Gamma_{\ell}|^2 = 1 + 2G_i' \Gamma_{\ell}' - 2G_i'' \Gamma_{\ell}'' + |G_i|^2 |\Gamma_{\ell}|^2. \quad (12)$$

Using eq (9), eq (8) can be rearranged and written as

$$\delta_{i\ell} g_{3\ell} g_{i1} = g_{i\ell} g_{31}, \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4. \end{matrix} \quad (13)$$

Next define  $f_{i\ell}$  as

$$f_{i\ell} = \delta_{i\ell} g_{3\ell} g_{i1} - g_{i\ell} g_{31} = 0, \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4, \end{matrix} \quad (14)$$

and expand  $f_{i\ell}$  in a Taylor series [7] about the best estimates of  $G_3$  and each  $G_i$ . Keeping only linear terms, eq (14) becomes

$$f_{i\ell} = f_{0i\ell} + \frac{\partial f_{i\ell}}{\partial G_3'} \Delta G_3' + \frac{\partial f_{i\ell}}{\partial G_3''} \Delta G_3'' + \frac{\partial f_{i\ell}}{\partial G_i'} \Delta G_i' + \frac{\partial f_{i\ell}}{\partial G_i''} \Delta G_i'' = 0, \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4, \end{matrix} \quad (15)$$

where  $f_{0i\ell}$  is the value of  $f_{i\ell}$  calculated from eq (14) using best estimates of  $G_3$  and  $G_i$ . The partial derivatives in eq (15) are obtained from eq (14);

$$\begin{aligned} \frac{\partial f_{i\ell}}{\partial G_3'} &= \delta_{i\ell} \frac{\partial g_{3\ell}}{\partial G_3'} g_{i1} - g_{i\ell} \frac{\partial g_{31}}{\partial G_3'} \\ \frac{\partial f_{i\ell}}{\partial G_3''} &= \delta_{i\ell} \frac{\partial g_{3\ell}}{\partial G_3''} g_{i1} - g_{i\ell} \frac{\partial g_{31}}{\partial G_3''} \\ \frac{\partial f_{i\ell}}{\partial G_i'} &= \delta_{i\ell} g_{3\ell} \frac{\partial g_{i1}}{\partial G_i'} - \frac{\partial g_{i\ell}}{\partial G_i'} g_{31} \\ \frac{\partial f_{i\ell}}{\partial G_i''} &= \delta_{i\ell} g_{3\ell} \frac{\partial g_{i1}}{\partial G_i''} - \frac{\partial g_{i\ell}}{\partial G_i''} g_{31} \end{aligned} \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4, \end{matrix} \quad (16)$$

where from eq (12),

$$\begin{aligned} \frac{\partial g_{i\ell}}{\partial G_i'} &= 2\Gamma_{\ell}' + 2G_i' |\Gamma_{\ell}|^2 \\ \frac{\partial g_{i\ell}}{\partial G_i''} &= -2\Gamma_{\ell}'' + 2G_i'' |\Gamma_{\ell}|^2 \end{aligned} \quad \begin{matrix} i = 3 \dots 6; \\ \ell = 1 \dots 4. \end{matrix} \quad (17)$$

These partial derivatives are calculated using the same best estimate of  $G_3$  and  $G_i$  used in calculating  $f_{0i\ell}$ .

The nine equations represented by eq (15) are solved for the eight unknown  $\Delta G_i'$  and  $\Delta G_i''$ . Since the equations are linear in these unknowns, the solution is straightforward. One solution is outlined in Appendix A. The  $\Delta G_i'$  and  $\Delta G_i''$  are then used to improve the previous estimate of the  $G_i'$  and  $G_i''$ .

$$\text{new } G_i' = \text{old } G_i' + \Delta G_i'$$

$$\text{new } G_i'' = \text{old } G_i'' + \Delta G_i'' \quad i = 3 \dots 6. (18)$$

These new estimates of  $G_i'$  and  $G_i''$  are used to compute new  $f_{oi\ell}$  and partial derivatives. The solution of eq (15) is then repeated for a new set of  $\Delta G_i'$  and  $\Delta G_i''$ . The iteration is continued until the  $\Delta G_i'$  and  $\Delta G_i''$  become insignificant.

#### B. Initial Estimate of the $G_i$

Since the solution of eq (8) for the  $G_i$  is an iteration process, estimates of the  $G_i$  are needed to begin the iteration. If the six-port is designed so that  $P_3$  is primarily a function of the incident wave, then  $G_3$  will be small. Also, we have assumed that  $r_1$  is small. Under these conditions, estimates of the  $G_i$  may be obtained by letting

$$G_3 = r_1 = 0. \quad (19)$$

Then eq (8) reduces to

$$\delta_{i\ell} = |1 + G_i r_\ell|^2 = g_{i\ell} \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 2, 3, 4 \end{matrix} \quad (20)$$

which has been expanded in eq (12). Let the three remaining terminations have a large constant reflection coefficient magnitude such as for three offset shorts. When  $|r_\ell|^2 = \text{constant}$  for  $\ell = 2, 3, 4$ , the three equations in eq (20) combine to give

$$\delta_{i2} - \delta_{i3} = 2G_i' (r_2' - r_3') - 2G_i'' (r_2'' - r_3'') \quad (21)$$

$$\delta_{i2} - \delta_{i4} = 2G_i' (r_2' - r_4') - 2G_i'' (r_2'' - r_4'') \quad (22)$$

which can be solved for  $G_i'$  and  $G_i''$ ,  $i = 4, 5, 6$ ;

$$2G_i' = \frac{(\delta_{i2} - \delta_{i3}) (r_2'' - r_4'') - (\delta_{i2} - \delta_{i4}) (r_2'' - r_3'')}{(r_2' - r_3') (r_2'' - r_4'') - (r_2' - r_4') (r_2'' - r_3'')}, \quad (23)$$

$$-2G_i'' = \frac{(r_2' - r_3') (\delta_{i2} - \delta_{i4}) - (r_2' - r_4') (\delta_{i2} - \delta_{i3})}{(r_2' - r_3') (r_2'' - r_4'') - (r_2' - r_4') (r_2'' - r_3'')} \quad (24)$$

Since all quantities on the right of eq (23) and eq (24) are known, estimates of  $G_i$  ( $i = 4, 5, 6$ ) can be calculated from these equations.

When one of the terminations is a flat short, and another termination is an open, eqs (23) and (24) can be simplified. Let

$\Gamma_2 = 1$  (open),  $\Gamma_3 = -1$  (short).

Then  $\Gamma_2'' = \Gamma_3'' = 0$ , and eq (23) and eq (24) reduce to

$$G_i' = \frac{\delta_{i2} - \delta_{i3}}{4} \quad (25)$$

$$G_i'' = \frac{2(\delta_{i2} - \delta_{i4}) - (1 - \Gamma_4')(\delta_{i2} - \delta_{i3})}{4\Gamma_4''} \quad (26)$$

Note that the value of  $G_i'$  is independent of  $\Gamma_4$ . It is possible to obtain  $G_i''$  independent of  $\Gamma_4$  also. For the short ( $\Gamma_3 = -1$ ), eq (20) gives

$$\delta_{i3} = (1 - G_i')^2 + G_i''^2 \quad (27)$$

from which

$$G_i''^2 = \delta_{i3} - (1 - G_i')^2 \quad (28)$$

where  $G_i'$  is obtained from eq (25). This gives  $G_i''$  independent of  $\Gamma_4$  except for a choice of sign. The sign of  $G_i''$  can be chosen to agree with that obtained for an ideal six-port corresponding to the design being used.

Equations (23) and (24), or eqs (25) and (26) or eq (28) give estimates of the  $G_i$  ( $i = 4, 5, 6$ ) to begin the iterative solution of eq (8) for the actual value of  $G_i$ .

#### IV. EQUATIONS FOR $\Gamma$

Once the  $G_i$  are determined, the ratios  $|A_i|^2/A_3|^2$  can be calculated from eq (7). Call these ratios  $K_i$ ;

$$K_i = \frac{|A_i|^2}{|A_3|^2} = \frac{P_{i1}}{P_{31}} \frac{|1 + G_3\Gamma_1|^2}{|1 + G_i\Gamma_1|^2}, \quad i = 4, 5, 6. \quad (29)$$

Then eq (7) can be used to obtain the reflection coefficient  $\Gamma_u$  of any other termination conn connected to the reference plane;

$$\frac{P_i}{P_3} = K_i \frac{|1 + G_i\Gamma_u|^2}{|1 + G_3\Gamma_u|^2} \quad i = 4, 5, 6. \quad (30)$$

The three equations given by eq (30) yield  $\Gamma_u$ .

With the  $G_i$  and  $K_i$  known, there are several ways to calculate  $\Gamma_u$ . The most accurate value of  $\Gamma_u$  is obtained by iterating the three equations in eq (30) to solve for the two unknown components  $\Gamma_u'$  and  $\Gamma_u''$  of  $\Gamma_u$ . A less accurate but closed linear solution may be obtained from the three equations in eq (30) by considering  $\Gamma_u'$ ,  $\Gamma_u''$ ,  $|\Gamma_u|^2$  to be three independent unknowns. A different linear solution can be obtained from eq (4). These three different ways of calculating  $\Gamma_u$  are outlined below.

##### A. Iterating to Find $\Gamma'$ and $\Gamma''$ .

The solution of eq (30) for  $\Gamma_u$  is similar to the solution of eq (8) for the  $G_i$ . Using eq (9) in eq (30), it can be rewritten

$$\rho_i g_3 = g_i, \quad i = 4,5,6, \quad (31)$$

where the second subscript on  $g$  has been dropped and  $\rho_i$  is defined as

$$\rho_i \equiv \frac{P_i}{P_3 K_i}, \quad i = 4,5,6. \quad (32)$$

Define  $f_i$  as

$$f_i = \rho_i g_3 - g_i = 0, \quad i = 4,5,6, \quad (33)$$

and expand  $f_i$  in a Taylor series about the best estimate of  $\Gamma_u$ ;

$$f_i = f_{0i} + \frac{\partial f_i}{\partial \Gamma_u'} \Delta \Gamma_u' + \frac{\partial f_i}{\partial \Gamma_u''} \Delta \Gamma_u'' \quad i = 4,5,6, \quad (34)$$

where  $f_{0i}$  is the value of  $f_i$  calculated from eq (33) using the best estimate of  $\Gamma_u$ . The partial derivatives

$$\frac{\partial f_i}{\partial \Gamma_u'} = \rho_i \frac{\partial g_3}{\partial \Gamma_u'} - \frac{\partial g_i}{\partial \Gamma_u'} = 2(\rho_i |G_3|^2 - |G_i|^2) \Gamma_u' + 2(\rho_i G_3' - G_i') \quad (35)$$

$$\frac{\partial f_i}{\partial \Gamma_u''} = \rho_i \frac{\partial g_3}{\partial \Gamma_u''} - \frac{\partial g_i}{\partial \Gamma_u''} = 2(\rho_i |G_3|^2 - |G_i|^2) \Gamma_u'' - 2(\rho_i G_3'' - G_i'') \quad (36)$$

for  $i = 4,5,6$  are also calculated using the same best estimate of  $\Gamma_u$ . The three equations represented by eq (34) are solved for the two unknowns  $\Delta \Gamma_u'$  and  $\Delta \Gamma_u''$  which are used to improve the previous estimate of  $\Gamma_u$ . The iteration is repeated until  $\Delta \Gamma_u'$  and  $\Delta \Gamma_u''$  become insignificant.

An initial estimate of  $\Gamma_u$  to begin the iteration with can be obtained from either of the two linear solutions given below.

#### B. Linear Solution of $\Gamma'$ , $\Gamma''$ , and $|\Gamma|^2$ .

A closed linear solution of eq (30) can be obtained by writing eq (30) in the form of eq (31) and expanding with eq (12). This leads to

$$\rho_i [1 + 2G_3' \Gamma_u' - 2G_3'' \Gamma_u'' + |G_3|^2 |\Gamma_u|^2] = 1 + 2G_i' \Gamma_u' - 2G_i'' \Gamma_u'' + |G_i|^2 |\Gamma_u|^2 \quad (37)$$

or

$$1 - \rho_i = 2(\rho_i G_3' - G_i') \Gamma_u' - 2(\rho_i G_3'' - G_i'') \Gamma_u'' + (\rho_i |G_3|^2 - |G_i|^2) |\Gamma_u|^2, \quad i = 4,5,6. \quad (38)$$

The three equations represented by eq (38) are linear in the three quantities  $\Gamma_u'$ ,  $\Gamma_u''$ ,  $|\Gamma_u|^2$ . The solution for these quantities is therefore straightforward. Note that the coefficients of  $\Gamma_u'$ ,  $\Gamma_u''$ , and  $|\Gamma_u|^2$  are the same terms needed to calculate the partials in eqs (35) and (36).



### C. Constant Matrix Solution for $r$ , $r''$ , and $|r|^2$ .

A closed matrix solution for  $r'$ ,  $r''$ , and  $|r|^2$  can be obtained directly from eqs. (1), (2), or (4). A derivation for these quantities beginning with eq (1) is given by Hoer [3]. A similar derivation beginning with eq (4) leads to the matrix equation

$$|a|^2 \begin{bmatrix} 1 \\ |r|^2 \\ r' \\ r'' \\ r \end{bmatrix} = \underline{G} \begin{bmatrix} p_3 \\ p_4 \\ p_5 \\ p_6 \end{bmatrix} \quad (39)$$

where  $\underline{G}$  is a real four-by-four matrix which is a function only of the calibration constants  $|A_3|$ ,  $G_j$ , and  $K_j$ ;

$$\underline{G} = \frac{1}{|A_3|^2} \begin{bmatrix} 1 & |G_3|^2 & 2G_3' & -2G_3'' \\ K_4 & K_4 |G_4|^2 & 2K_4 G_4' & -2K_4 G_4'' \\ K_5 & K_5 |G_5|^2 & 2K_5 G_5' & -2K_5 G_5'' \\ K_6 & K_6 |G_6|^2 & 2K_6 G_6' & -2K_6 G_6'' \end{bmatrix}^{-1} \quad (40)$$

The reflection coefficient is obtained from elements 1, 3, and 4 of the left column vector in eq (39), i.e., from  $|a|^2$ ,  $|a|^2 r'$ , and  $|a|^2 r''$ ;

$$r = \frac{r' |a|^2 + j r'' |a|^2}{|a|^2} \quad (41)$$

Since  $|A_3|^2$  in eq (40) cancels when calculating  $r$  with eq (41), it can be set equal to one.

### D. Comparison of Solutions for $r$

The iterative method in A is more accurate than either of the closed linear solutions described in B or C. This is because all three equations in eq (30) are used to find only two instead of three unknowns. When  $r'$ ,  $r''$ , and  $|r|^2$  are considered to be three independent unknowns, these three values will not usually satisfy the relation

$$r'^2 + r''^2 = |r|^2.$$

However, the loss in accuracy may not be significant or worth the extra time required to iterate.

One advantage of solution C over the other two solutions is that the matrix  $\underline{G}$  is independent of  $r$  and therefore needs to be calculated only once at a given frequency for any number of measurements.

## V. CALIBRATION EQUATIONS, $v$ and $i$ PARAMETERS

Instead of expressing the equations in terms of the reflection coefficient at the reference plane, it is sometimes more convenient to write the equations in terms of impedance. This is especially true when a high quality flat short is one of the four standard terminations used in calibrating the six-port. If in eq (1) we let

$$v = a+b \quad (42)$$

$$iZ_0 = a-b \quad (43)$$

then eq (1) becomes

$$P_i = |C_i v + D_i i Z_0|^2, \quad i = 3 \dots 6, \quad (44)$$

where  $v, i$ , and  $Z_0$  are the voltage, current, and characteristic impedance at the reference plane, and

$$C_i = \frac{A_i + B_i}{2}, \quad D_i = \frac{A_i - B_i}{2} \quad i = 3 \dots 6. \quad (45)$$

Now add a subscript  $\ell$  as before to indicate the termination being used, and factor out  $D_i i Z_0$  from eq (44) to obtain an expression similar to eq (4);

$$P_{i\ell} = |D_i i_\ell Z_0|^2 |1 + H_i z_\ell|^2 \quad \begin{matrix} i = 3 \dots 6; \\ \ell = 1 \dots 4, \end{matrix} \quad (46)$$

where  $z_\ell$  is the impedance  $Z_\ell$  of the termination at the reference plane divided by  $Z_0$ , and  $H_i$  is a new constant describing the six-port;

$$z_\ell = \frac{v_\ell}{i_\ell Z_0} = \frac{Z_\ell}{Z_0} \quad (47)$$

$$H_i = \frac{C_i}{D_i} = \frac{1 + G_i}{1 - G_i} \quad (48)$$

Again assume that  $P_3$  is primarily a function of the incident wave,  $a$ , so that  $P_3$  will never be zero. Dividing eq (46) by  $P_{3\ell}$  gives

$$\frac{P_{i\ell}}{P_{3\ell}} = \frac{|D_i|^2}{|D_3|^2} \frac{|1 + H_i z_\ell|^2}{|1 + H_3 z_\ell|^2} \quad \begin{matrix} i = 4, 5, 6; \\ \ell = 1 \dots 4. \end{matrix} \quad (49)$$

For the first termination, eq (49) gives

$$\frac{P_{i1}}{P_{31}} = \frac{|D_i|^2}{|D_3|^2} \frac{|1 + H_i z_1|^2}{|1 + H_3 z_1|^2} \quad i = 4, 5, 6. \quad (50)$$

Finally, assume again that  $z_1$  of the first termination is such that none of the  $P_{i1}$ , are zero. Then dividing eq (49) by eq (50) yields

$$\delta_{i\ell} = \frac{P_{i\ell} P_{31}}{P_{3\ell} P_{i1}} = \left| \frac{1 + H_i z_\ell}{1 + H_3 z_\ell} \cdot \frac{1 + H_3 z_1}{1 + H_i z_1} \right|^2 \quad \begin{array}{l} i = 4,5,6 \\ \ell = 2,3,4. \end{array} \quad (51)$$

In this solution of this equation for the  $H_i$  is identical to the solution of eq (8) for the  $G_i$ . Initial estimates of the  $H_i$  can be obtained from initial estimates of the  $G_i$  through eq (48), or from equation given below.

## VI. SIMPLIFIED CALIBRATION EQUATIONS

### A. Ideal Short

Choose the first termination to be a high quality flat short so that it can be assumed that  $Z_1=0$ . Then eq (51) becomes

$$\delta_{i\ell} = \frac{|1 + H_i z_\ell|^2}{|1 + H_3 z_\ell|^2} \quad \begin{array}{l} i = 4,5,6; \\ \ell = 2,3,4. \end{array} \quad (52)$$

Since this equation assumes that none of the  $P_{i1}$  are zero, none of the sidearms can be proportional to  $v = a+b$  since  $v$  is zero when a short is at the reference plane. Although eq (52) is also a nonlinear equation, it is somewhat easier to solve for the calibration constants than in eq (51) or eq (8).

No assumption about the remaining three terminations are made in eq (52). The value of  $Z_\ell$  for these three remaining known terminations could be an open, a reactance, and a resistance. If these three terminations are sufficiently ideal, the solution can be simplified as described below.

### B. Ideal Open, Reactance, and Resistance

If the second termination is an open circuit,  $z_\ell$  becomes infinite so eq (52) gives

$$\delta_{i2} = \frac{|H_i|^2}{|H_3|^2} \quad i = 4,5,6. \quad (53)$$

Let the third termination be a pure reactance, and the fourth termination be a pure resistance. Then if we define

$$H_i = H_i' + jH_i'' \quad (54)$$

$$z_\ell = R_\ell + jX_\ell, \quad (55)$$

and assume that  $Z_0$  is real, eq (52) yields

$$\delta_{i3} = \frac{|1 + H_i jX_3|^2}{|1 + H_3 jX_3|^2}, \quad i = 4,5,6, \quad (56)$$

$$\delta_{i4} = \frac{|1 + H_i R_4|^2}{|1 + H_3 R_4|^2}, \quad i = 4,5,6. \quad (57)$$

Using eqs (53) and (54) in eqs (56) and (57) leads to

$$\delta_{i3} = \frac{1 - 2 H_i'' x_3 + \delta_{i2} |H_3|^2 x_3^2}{1 - 2 H_3'' x_3 + |H_3|^2 x_3^2} \quad i = 4,5,6, \quad (58)$$

$$\delta_{i4} = \frac{1 + 2 H_i' R_4 + \delta_{i2} |H_3|^2 R_4^2}{1 + 2 H_3' R_4 + |H_3|^2 R_4^2} \quad i = 4,5,6 \quad (59)$$

Solving eq (58) for  $H_i''$  and eq (59) for  $H_i'$  yields

$$H_i'' = \frac{1 - \delta_{i3}}{2 x_3} + \delta_{i3} H_3'' + x_3 \frac{(\delta_{i2} - \delta_{i3})}{2} |H_3|^2 \quad (60)$$

$$H_i' = \frac{\delta_{i4} - 1}{2 R_4} + \delta_{i4} H_3' + R_4 \frac{(\delta_{i4} - \delta_{i2})}{2} |H_3|^2 \quad (61)$$

for  $i = 4,5,6$ . Finally, adding the square of eq (60) to the square of eq (61) and substituting into eq (53) gives

$$\begin{aligned} (H_i'')^2 + (H_i')^2 &= |H_i|^2 = \\ \delta_{i2} |H_3|^2 &= \left[ \frac{1 - \delta_{i3}}{2 x_3} + \delta_{i3} H_3'' + x_3 \frac{(\delta_{i2} - \delta_{i3})}{2} |H_3|^2 \right]^2 \\ &+ \left[ \frac{\delta_{i4} - 1}{2 R_4} + \delta_{i4} H_3' + R_4 \frac{(\delta_{i4} - \delta_{i2})}{2} |H_3|^2 \right]^2 \quad i = 4,5,6. \quad (62) \end{aligned}$$

The three equations represented by eq (62) can be solved for  $H_3'$  and  $H_3''$ . The remaining  $H_i'$  and  $H_i''$  for  $i = 4,5,6$  are then obtained from eqs (60) and (61). Although eq (62) is a nonlinear equation and must be solved by iteration, the iteration is faster than when solving eqs (8), (51) and (52) because only two unknowns are being solved for.

### C. Initial Estimates of $H_3$

We have already noted that  $G_3$  is small for a six-port designed so that  $P_3$  is primarily a function of the incident wave. For this design eq (48) gives

$$H_3 \approx 1 + j0.$$

This value of  $H_3$  is a good estimate to use in beginning the iterative solution of eq (62).

## VII. EQUATIONS FOR Z

Once the  $H_i$  are determined, the ratios  $|D_i|^2/|D_3|^2$  can be calculated from eq (50). Call these ratios small  $k_i$ ;

$$k_i = \frac{|D_i|^2}{|D_3|^2} = \frac{P_{i1}}{P_{31}} \frac{|1 + H_3 z_1|^2}{|1 + H_i z_1|^2} \quad i = 4, 5, 6. \quad (64)$$

Then eq (50) can be used to obtain the normalized impedance  $z_u$  of any other termination connected to the reference plane;

$$\frac{P_i}{P_3} = k_i \frac{|1 + H_i z_u|^2}{|1 + H_3 z_u|^2} \quad i = 4, 5, 6. \quad (65)$$

These three equations can be solved for  $z_u$  in the same manner as eq (30) was solved for  $\Gamma_u$ . One can iterate to find  $R_u$  and  $X_u$  as outlined in section IV A, or derive a linear solution for  $R_u$ ,  $X_u$ , and  $|z_u|^2$  as outlined in section IV B. A linear solution for  $|v|$ ,  $|iZ_0|$ ,  $R_u$  and  $X_u$  is similar to that out-lined in section IV C and is given below.

### A. Constant Matrix Solution for R, X, and $|z|^2$ .

A closed matrix solution  $R$ ,  $X$ , and  $|z|^2$  at the reference plane can be obtained from eq (46). Dropping the subscript  $z$  and expanding eq (46) gives

$$P_i = |D_i Z_0|^2 \left[ 1 + 2H_i' R - 2H_i'' X + |H_i|^2 |z|^2 \right]. \quad (66)$$

Using eq (64) in eq (66),

$$P_i = |D_3|^2 |iZ_0|^2 \left[ K_i + 2K_i H_i' R - 2K_i H_i'' X + K_i |H_i|^2 |z|^2 \right], \quad i = 3 \dots 6. \quad (67)$$

The four equations represented by eq (67) lead to the matrix equation

$$|iZ_0|^2 \begin{bmatrix} |z|^2 \\ 1 \\ R \\ X \end{bmatrix} = \underline{H} \begin{bmatrix} P_3 \\ P_4 \\ P_5 \\ P_6 \end{bmatrix} \quad (68)$$

where  $\underline{H}$  is a constant matrix similar to  $\underline{G}$  and is a function only of the calibration constants  $|D_3|$ ,  $H_i$ , and  $k_i$ ;



$$\underline{H} = \frac{1}{|D_3|^2} \begin{bmatrix} |H_3|^2 & 1 & 2 H_3' & -2 H_3'' \\ k_4 |H_4|^2 & k_4 & 2 k_4 H_4' & -2 k_4 H_4'' \\ k_5 |H_5|^2 & k_5 & 2 k_5 H_5' & -2 k_5 H_5'' \\ k_6 |H_6|^2 & k_6 & 2 k_6 H_6' & -2 k_6 H_6'' \end{bmatrix}^{-1} \quad (69)$$

The impedance is obtained from elements 2, 3, and 4 of the left column vector in eq (68);

$$z_u = \frac{Z_u}{Z_0} = \frac{|iZ_0|^2 R + J |iZ_0|^2 X}{|iZ_0|^2} \quad (70)$$

Since  $|D_3|^2$  in eq (69) cancels when calculating  $z_u$  with eq (70), it can be set equal to one.

It can be shown that  $\underline{H}$  and  $\underline{G}$  are related by [3]

$$\underline{H} = \underline{K} \underline{G} \quad (71)$$

where

$$\underline{K} = \begin{bmatrix} 1 & 1 & 2 & 0 \\ 1 & 1 & -2 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 2 \end{bmatrix} \quad (72)$$

## VIII. CONCLUSION

Equations have been derived for determining the calibration constant of a six-port reflectometer and also for calculating  $\Gamma$  or  $z$  once these constants are known. Further work needs to be done to determine how much accuracy is lost when using the closed linear solutions for  $\Gamma$  or  $z$  instead of the nonlinear iterative solution.

The equations given in this report can be extended to the case of more than 6 detectors or when more than four known terminations are available by letting  $i = 3, 4, 5, 6, 7, \dots$  and/or  $\ell = 1, 2, 3, 4, 5, \dots$

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# APPENDIX A

This appendix outlines a solution of eq (15) for the eight  $\Delta G$ , and also gives useful some approximations to simplify the solution.

If the first standard termination has a reflection coefficient  $\Gamma_1 \approx 0$ , then eqs (12) and (17) become

$$g_{i1} \approx 1, \quad i = 3 \dots 6 \quad (A1)$$

$$\frac{\partial g_{i1}}{\partial G_i'} \approx \frac{\partial g_{i1}}{\partial G_i''} \approx 0 \quad i = 3 \dots 6, \quad (A2)$$

which can be used to simplify the partial derivative in eq (16) to

$$\begin{aligned} \frac{\partial f_{i\ell}}{\partial G_3'} &= \delta_{i\ell} \frac{\partial g_{3\ell}}{\partial G_3'} \\ \frac{\partial f_{i\ell}}{\partial G_3''} &= \delta_{i\ell} \frac{\partial g_{3\ell}}{\partial G_3''} \\ \frac{\partial f_{i\ell}}{\partial G_i'} &= - \frac{\partial g_{i\ell}}{\partial G_i'} \\ \frac{\partial f_{i\ell}}{\partial G_i''} &= - \frac{\partial g_{i\ell}}{\partial G_i''} \end{aligned} \quad \begin{aligned} i &= 4, 5, 6 \\ \ell &= 2, 3, 4. \end{aligned} \quad (A3)$$

To simplify writing, define

$$\begin{aligned} K_{i\ell} &\equiv \frac{\partial g_{i\ell}}{\partial G_i'} = 2\Gamma_\ell' + 2G_i' |\Gamma_\ell|^2 \\ L_{i\ell} &\equiv \frac{\partial g_{i\ell}}{\partial G_i''} = -2\Gamma_\ell'' + 2G_i'' |\Gamma_\ell|^2 \end{aligned} \quad \begin{aligned} i &= 3 \dots 6, \\ \ell &= 1 \dots 4. \end{aligned} \quad (A4)$$

where eq (12) was used to obtain the partials. Substituting eqs (A3) and (A4) into eq (15) gives

$$f_{oi\ell} + \delta_{i\ell} K_{3\ell} \Delta G_3' + \delta_{i\ell} L_{3\ell} \Delta G_3'' = K_{i\ell} \Delta G_i' + L_{i\ell} \Delta G_i'' \quad \begin{aligned} i &= 4, 5, 6; \\ \ell &= 2, 3, 4. \end{aligned} \quad (A5)$$

One way of solving this equation for each  $\Delta G$  is to first eliminate  $\Delta G_i'$  and  $\Delta G_i''$  for  $i = 4, 5, 6$ , and then solve for  $\Delta G_3'$  and  $\Delta G_3''$ . The two equations obtained from eq (A5) for measurements with termination numbers two and three can be written as one matrix equation;

$$\begin{bmatrix} f_{oi2} \\ f_{oi3} \end{bmatrix} + \begin{bmatrix} \delta_{i2} K_{32} & \delta_{i2} L_{32} \\ \delta_{i3} K_{33} & \delta_{i3} L_{33} \end{bmatrix} \begin{bmatrix} \Delta G_3' \\ \Delta G_3'' \end{bmatrix} = \begin{bmatrix} K_{i2} & L_{i2} \\ K_{i3} & L_{i3} \end{bmatrix} \begin{bmatrix} \Delta G_i' \\ \Delta G_i'' \end{bmatrix}$$

$$i = 4, 5, 6. \quad (A6)$$

or simply

$$\vec{F}_i + \underline{M}_i \vec{\Delta G}_3 = \underline{N}_i \vec{\Delta G}_i,$$

$$i = 4, 5, 6 \quad (A7)$$

where the matrix symbols in (A7) are defined by the corresponding matrices in eq (A6). Solving eq (A7) for  $\vec{\Delta G}_i$ ,

$$\vec{\Delta G}_i = \underline{N}_i^{-1} \vec{F}_i + \underline{N}_i^{-1} \underline{M}_i \vec{\Delta G}_3$$

$$i = 4, 5, 6. \quad (A8)$$

Equations (A5) for the measurement with termination number four can also be written as a matrix equation;

$$f_{oi4} + \underline{S}_i \vec{\Delta G}_3 = \underline{T}_i \vec{\Delta G}_i$$

$$i = 4, 5, 6 \quad (A9)$$

where  $\underline{S}_i$  and  $\underline{T}_i$  are 1-by-2 matrices defined by

$$\underline{S}_i = \begin{bmatrix} \delta_{i4} K_{34} & \delta_{i4} L_{34} \end{bmatrix}$$

$$(A10)$$

$$\underline{T}_i = \begin{bmatrix} K_{i4} & L_{i4} \end{bmatrix}.$$

$$(A11)$$

Substituting eq (A8) into eq (A9) yields

$$f_{oi4} + \underline{S}_i \vec{\Delta G}_3 = \underline{T}_i (\underline{N}_i^{-1} \vec{F}_i + \underline{N}_i^{-1} \underline{M}_i \vec{\Delta G}_3)$$

$$i = 4, 5, 6 \quad (A12)$$

or

$$f_{oi4} + (\underline{S}_i - \underline{T}_i \underline{N}_i^{-1} \underline{M}_i) \vec{\Delta G}_3 = \underline{T}_i \underline{N}_i^{-1} \vec{F}_i$$

$$i = 4, 5, 6. \quad (A13)$$

The three equations represented by eq (A13) can be combined into one matrix equation;

$$\begin{bmatrix} f_{o44} \\ f_{o54} \\ f_{o64} \end{bmatrix} + \begin{bmatrix} \underline{S}_4 - \underline{T}_4 \underline{N}_4^{-1} \underline{M}_4 \\ \underline{S}_5 - \underline{T}_5 \underline{N}_5^{-1} \underline{M}_5 \\ \underline{S}_6 - \underline{T}_6 \underline{N}_6^{-1} \underline{M}_6 \end{bmatrix} \vec{\Delta G}_3 = \begin{bmatrix} \underline{T}_4 \underline{N}_4^{-1} \underline{F}_4 \\ \underline{T}_5 \underline{N}_5^{-1} \underline{F}_5 \\ \underline{T}_6 \underline{N}_6^{-1} \underline{F}_6 \end{bmatrix} \quad (A14)$$

or simply

$$\vec{U} + \underline{V} \vec{\Delta G}_3 = \vec{W}. \quad (A15)$$

The solution for  $\vec{\Delta G}_3$  is

$$\vec{\Delta G}_3 = (\underline{V}^T \underline{V})^{-1} \underline{V}^T (\vec{W} - \vec{U}). \quad (A16)$$

With  $\vec{\Delta G}_3$  known, the remaining  $\vec{\Delta G}_i$  for  $i = 4, 5, 6$  can be obtained from eq (A8).



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